

What should an elementary math classroom look like in 2019?

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October 2018

Agenda

- Classroom environment
- The math to focus on
- Consolidating the math in a lesson
- Critical thinking
- Differentiation of instruction

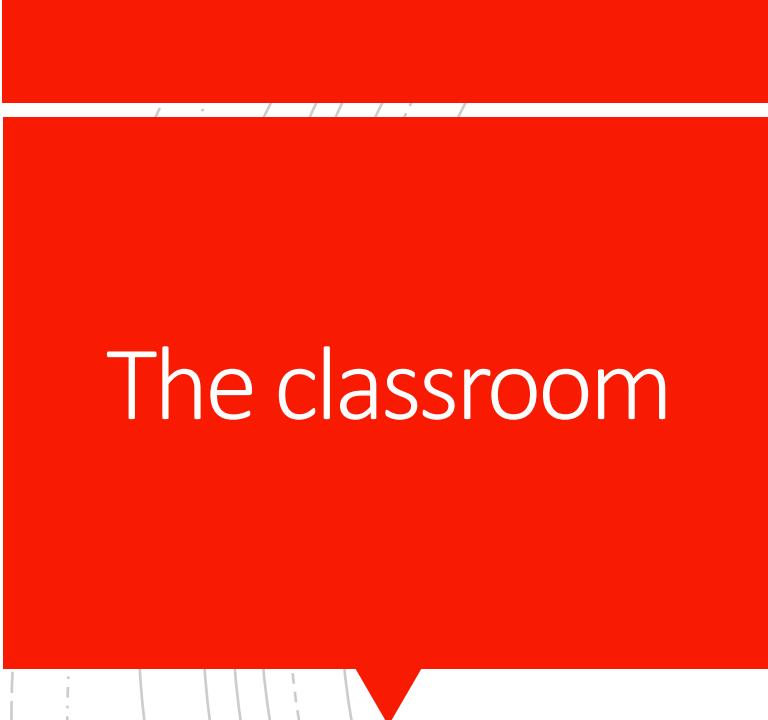
The classroom

- Lots of student conversation /debate about mathematics
- Kids working in pairs/groups
- e.g., I might ask:

The classroom

- Jason says that you can't get a little answer when you subtract two big numbers.
- Lia says you can.
- With whom do you agree? Why?

OR



The classroom

- It's always easier to add littler numbers.

The classroom

2 truths and a lie— which is the lie?

- 1.** There is no number in the 90s that you can represent with 3 more base ten units than rods.
- 2.** The only way to represent 47 is with 11 base ten blocks.
- 3.** You can represent 22 with 13 base ten blocks.

The classroom

- A safe environment- mistakes not a big deal
- Lots of use of thinking tools, whether manipulatives or technology

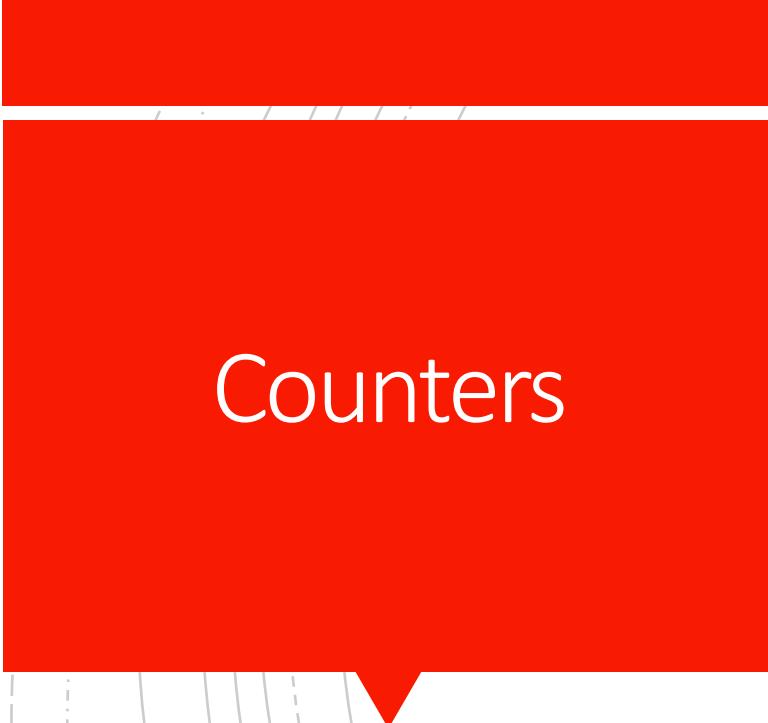


Lots of tools

- Thoughtful use of both manipulatives and digital resources

Counters

- Take 20 counters.
- How can you arrange them in 3 piles so that the piles are close to equal in size?
- How can you arrange them in 2 piles so that one pile is about twice as high as another pile?



Counters

- Take 20 counters.
- How can you arrange them in 3 piles so that there is 1 really big pile and 2 small ones?

Counters

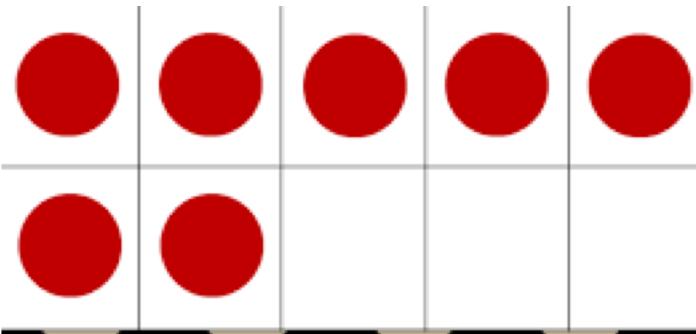
- You have red, blue and green counters.
- You have 2 more red ones than blue ones.
- You have 3 more green ones than blue ones.
- How many of each colour might you have?
- How many altogether?

Counters

- You can show a number by putting out counters in the form of a triangle.
- What numbers can you make?
- Which are harder to make?

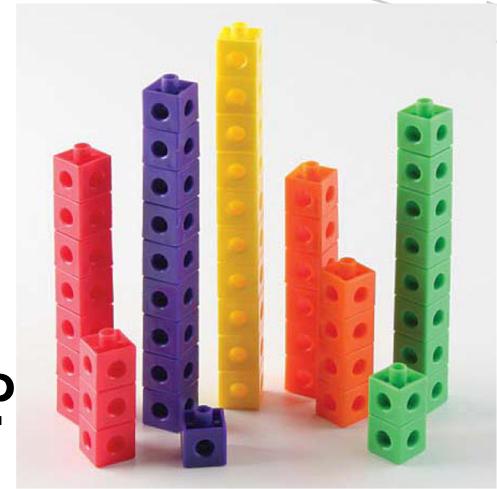
Ten-frames

- How could you use 10-frames to help you figure out pairs of numbers that add to 10?
- How could you use 10-frames to show why $8 + 9 = 17$?
- What numbers could you show if you fill 3 ten-frames and part of a fourth one?



Linking cubes

- How could you show 43?
- How could you show that $12 - 4 = 13 - 5$?
- What total lengths can you have if you use 3 colours and consecutive amounts for the colours?



Hundred chart

- What number might be in the bottom left quarter of the chart?
- What numbers is 34 near?
- How could you use the chart to add $43 + 25$?

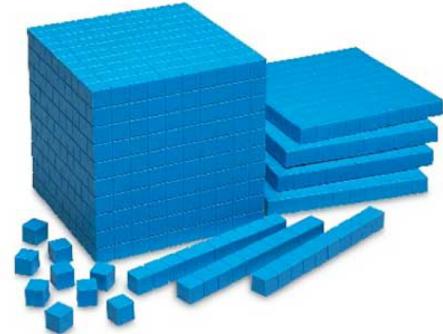
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Hundred chart

- How could you use the chart to figure out $62 - 18$?
- What would happen if you coloured all numbers including the digit 2?

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Base ten blocks



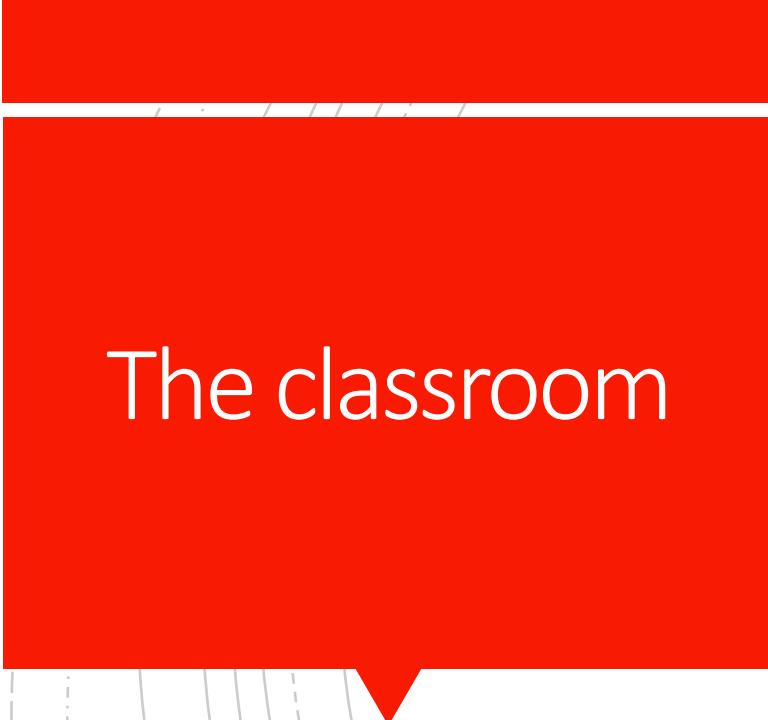
- What numbers can you represent with 12 blocks?
- What numbers can you represent with a lot of sticks and only a few small cubes?
- How can you use the blocks to figure out $132 - 48$?

Fraction Tower

1									
$\frac{1}{2}$					$\frac{1}{2}$				
$\frac{1}{3}$			$\frac{1}{3}$			$\frac{1}{3}$			
$\frac{1}{4}$		$\frac{1}{4}$		$\frac{1}{4}$		$\frac{1}{4}$			
$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{5}$		$\frac{1}{5}$	
$\frac{1}{6}$		$\frac{1}{6}$		$\frac{1}{6}$		$\frac{1}{6}$		$\frac{1}{6}$	
$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$	
$\frac{1}{9}$		$\frac{1}{9}$		$\frac{1}{9}$		$\frac{1}{9}$		$\frac{1}{9}$	
$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$	
$\frac{1}{12}$		$\frac{1}{12}$		$\frac{1}{12}$		$\frac{1}{12}$		$\frac{1}{12}$	
$\frac{1}{15}$		$\frac{1}{15}$		$\frac{1}{15}$		$\frac{1}{15}$		$\frac{1}{15}$	
$\frac{1}{18}$		$\frac{1}{18}$		$\frac{1}{18}$		$\frac{1}{18}$		$\frac{1}{18}$	
$\frac{1}{20}$		$\frac{1}{20}$		$\frac{1}{20}$		$\frac{1}{20}$		$\frac{1}{20}$	

Fraction Strips

- What do fractions that are $3/[]$ look like?
- Name fractions a little more than $2/3$.
- What equivalent fractions do you see?



The classroom

- Teachers leave the “work” to the students.
- High expectations



The classroom

Curiosity is piqued.

- How long is long hair?
- What is a number that takes a lot of words to say?
- How many pop cans would it take to balance a basketball?

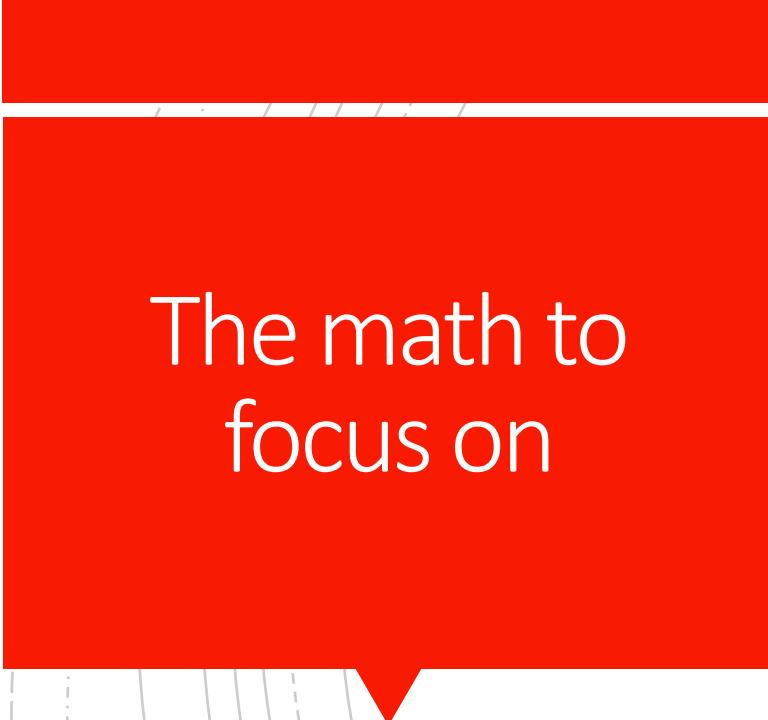
The classroom

- Accessible tasks with high ceilings
- I might ask:
- Choose two numbers so that when you add them, the answer is double (two of what you get) when you subtract them.
- Come up with at least a few answers.



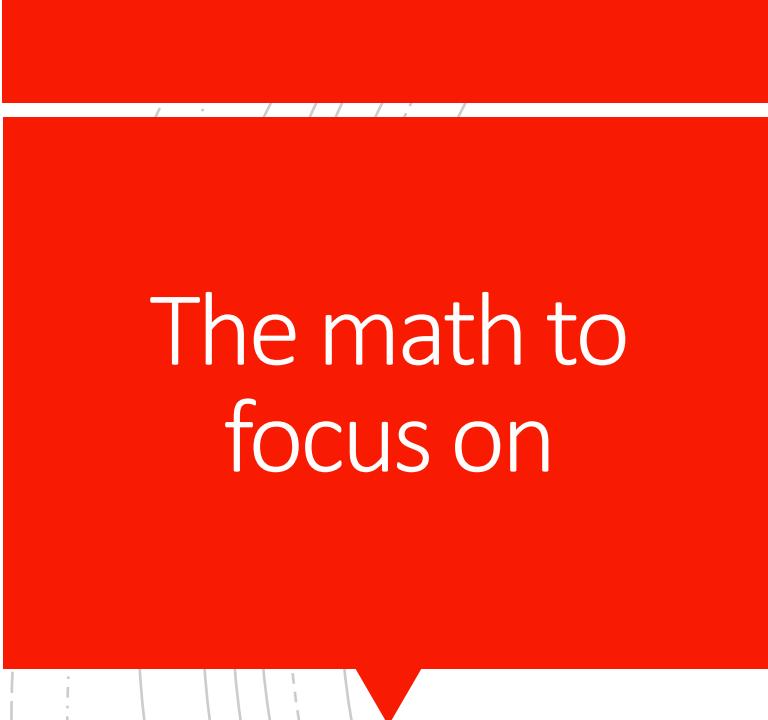
The classroom

- Feedback – more questions, less marks



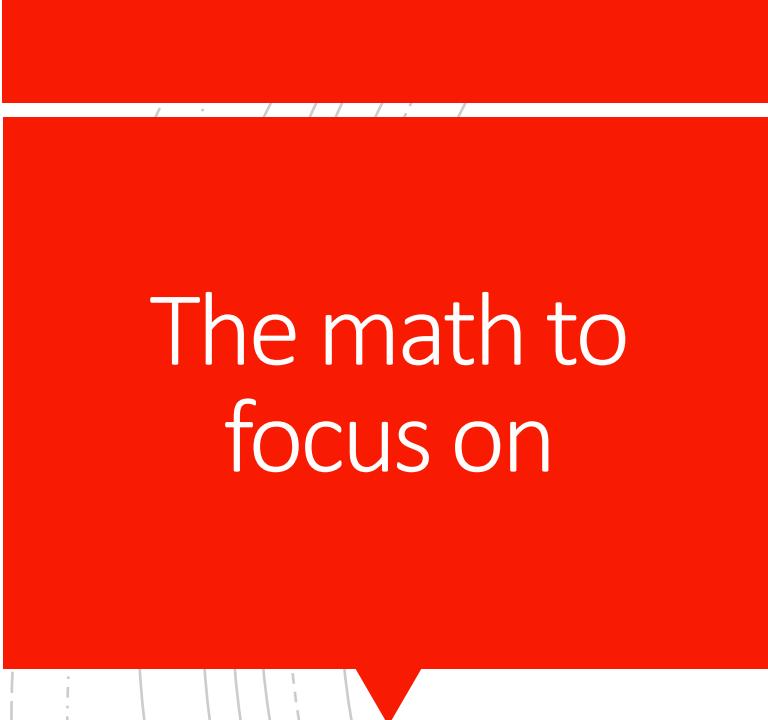
The math to focus on

- Each outcome requires “interpretation”.
- Teachers have to decide they are focusing on what is important.



The math to focus on

- For example... Grade 1 Length
- Students will be expected to demonstrate an understanding of measurement as a process of comparing by:
 - -identifying attributes that can be compared
 - - ordering objects
 - - making statements of comparison
 - - filling, covering or matching



The math to focus on

- Performance indicators
- Identify common attributes, such as length,.... that can be used to compare a given set of two objects.
- Compare and order two given objects and identify the attributes used to compare.
- Predict which object in a set is longest/shortest, determining by matching and explain the reasoning.



It might be

- Do they always have to predict longest/shortest or only some times?
- Should there ever be indirect measurement? How much if any?
- Should we “trick” kids with wiggle or curly things or items hidden behind barriers?
- Should there be more emphasis on comparing or ordering?



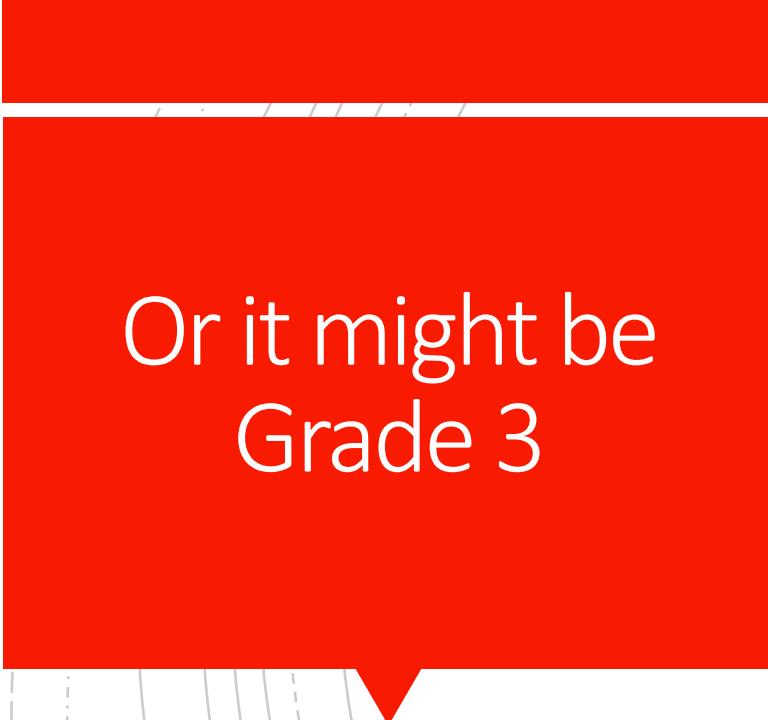
So a task might
be

- One object looks longer than another, but it really isn't.
- What could they be and why would that happen?



Or it might be

- How could you figure out whether the window is taller than how wide the whiteboard is?



Or it might be
Grade 3

- Students will be expected to demonstrate an understanding of fractions by:
- Explaining that a fraction represents a part of a whole
- Describing situations in which fractions are used
- Comparing fractions of the same whole with like denominators.

Performance indicators

- Describe everyday situations where fractions are used.
- Represent a given fraction concretely or pictorially.
- Identify, model and explain the meaning of the numerator and denominator.
- Sort a given set of diagrams of regions into those that represent equal parts and those that do not, and explain the sorting.

Performance indicators

- Name and record the fraction represented by the shaded and non-shaded parts of a given region.
- Compare given fractions with the same denominator using models.



It might be

- Does that mean we avoid fractions like fifths which rarely, if ever, occur in everyday life?
- Is the only model areas or regions or do we want number lines or masses or capacities, too?
- How important are the terms numerator and denominator?
- Do we focus on exact with pre-divided amounts or do we focus on estimation?
- Do we ask as much for “which is less?” as “which is more?”



So my task
might be

- A pizza is cut into 8 slices.
- Andy had 3 fewer slices than Brent.
- What fraction of the pizza could each have?
- OR

So my task
might be

- What fractions might make sense for this dot? Why?



Consolidating the math

- When we teach a lesson, there are ideas we want to ensure students meet.
- Without “lecturing”, how do we set a task for students to do and then make sure those ideas come to the surface?

Grade 2 example

- I am teaching a lesson about using personal strategies to subtract numbers under 100.
- I want students to focus on the strategies and why they work and why they are selected.

My task

- I was solving two different subtraction problems and the answers were both 15.
- But I figured out the two answers really different ways.
- What numbers might have been involved in my problems and why would I have used different ways?

My consolidation

- What could the equations have been if there was a subtraction and the answer was 15?
- Why might someone say that it is much easier to figure out $30 - 15$ than $41 - 26$? Do you think it is?
- Would you use the same strategy to solve these: $55 - 40$ and $32 - 17$? Explain what you would do each time.

Critical thinking

- There are two plates of cookies.
- One has a LOT more cookies than the other.
- How many might be on each plate?

Critical thinking

- You show a number with a LOT more ten rods than one cubes.
- What could the number be?

Critical thinking

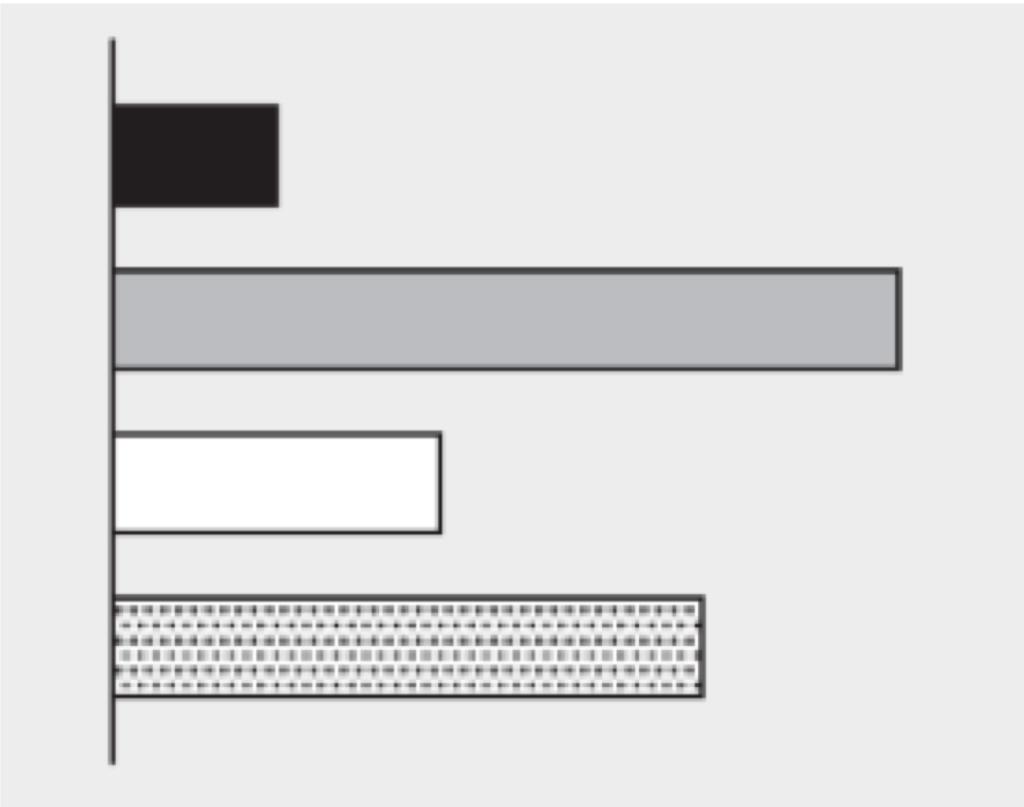
- An amount you can show with 6 coins is added to an amount you can show with 3 coins.
- How many coins might you NEED to show the sum?

Critical thinking

- Which is a better description of how far away your birthday is?
- Is it 50 days?
- Is it about 7 weeks?
- Is it almost 2 months?
- Why is it better?



Critical thinking





Critical thinking

- How could 1000 be a lot?
- How could it be a little?



Critical thinking

- Who doesn't belong?

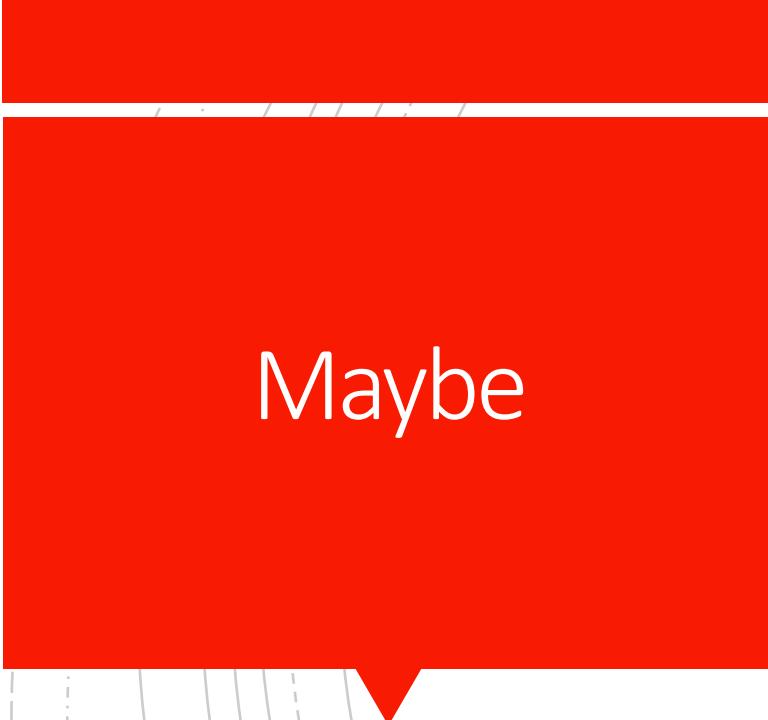
- 11
- 14
- 23
- 17

Differentiation

- The strategy I count on the most is the use of open questions.
- I also use parallel tasks.

Open questions

- The answer is 100.
- What might the question have been?



Maybe

- How old is really old?
- What is the first 3-digit number?
- What is 10 tens?
- What comes after 99?
- What is a perfect score on a test?



More examples

- There are a LOT of people in a car. How many might that be?
- There are NOT MANY students in a school. How many might there be?

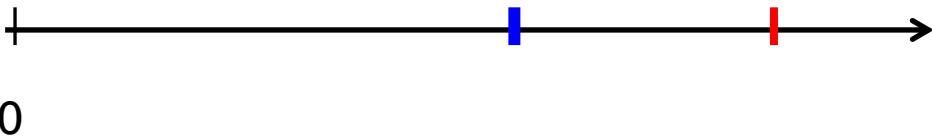


More examples

- The 10th shape in a pattern is a red triangle.
- What could the pattern look like?

More examples

- Choose a number for the red mark. Then choose an appropriate number for the blue mark.





More examples

- A number is just A LITTLE more than $\frac{1}{2}$.
- What might it be?

More examples

- _____ is 4 more than _____.
- What could go in the blanks to make this true?

- Then, ask:
 - Was the first number bigger or the second one?
 - Could the first number have been 20?
 - Could the two numbers be on different lines on a 100 chart?

More examples

- You buy an item and give the clerk one bill. Your change is one bill and 6 coins.
- What might the price have been?

Parallel tasks

- Very similar tasks that differ only in complexity, but address the same ideas.
- They can be debriefed using common questions.
- For example...

- Choice 1:*** Choose a number to subtract from 20. Draw two different pictures that would help you figure out the result.
- Choice 2:*** Choose a number to subtract from 5. Draw two different pictures that would help you figure out the result.

- How did you decide what number to choose?
- Could you have predicted about how much your answer would be?
- How do the pictures show the subtraction?
- How are your pictures alike? How are they different?

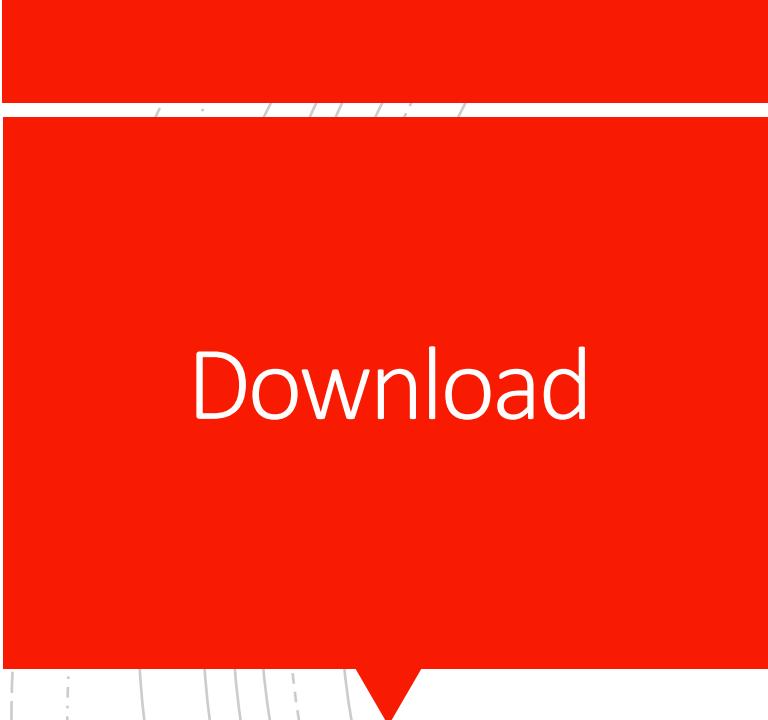
- Choice 1:*** Choose two 3-digit numbers to add for a total close to 400. How could you use base ten blocks to help you add?
- Choice 2:*** Choose two 2-digit numbers to add for a total close to 40. How could you use base ten blocks to help you add?

- How would you model the total you were trying to get close to?
- What would you do to show a number close to that number?
- How did you select the two numbers to make that total?
- How did using the blocks make the problem easier to solve?



Any questions

- Do you have additional questions you would like to discuss?



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