

Leadership in School Math

March, 2018

Agenda

- Part 1: How do you start?
 - Being intentional in going in the right direction
 - Being coherent
- Part 2: Finding out where your staff is
 - In terms of beliefs
 - By looking at common tasks
- Part 3: Look Fors
 - What to look for in classrooms
 - What to look for in conversations with staff

Agenda

- Part 4: How should lessons look?
 - What should learning goals look like?
 - What should consolidation look like?
 - What should differentiation look like?
- Part 5: Questions

Part 1:

How Do You Start?

Part 1

- Teachers must choose PURPOSEFUL activities that lead students to MATHEMATICAL insight and understanding.

Try This Problem That Might Be Used in a Grade 2 Classroom

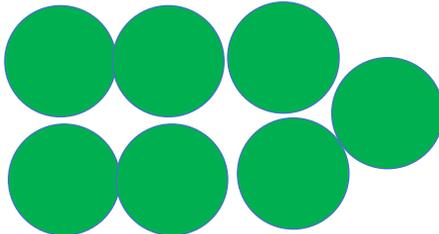
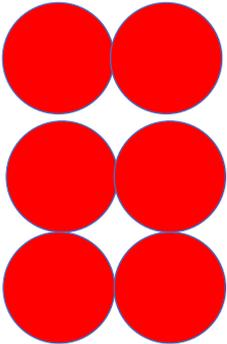
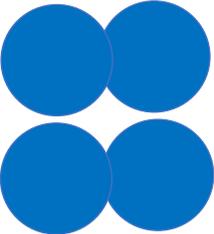
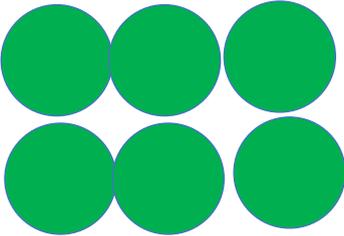
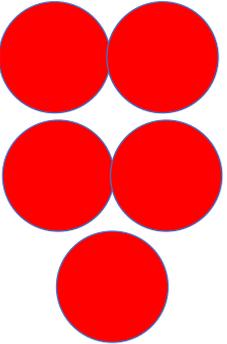
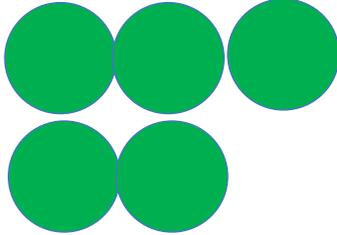
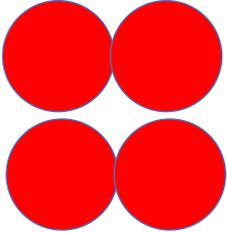
- Choose between 20 and 40 counters.
- The amount you choose must be used for ALL parts of the task.

Decomposing

- Which way of decomposing will work with your number of counters?
 - 3 equal groups.
 - 2 groups — one exactly double the other.
 - 1 big group and 2 small ones.

Variation for Grade 1

- You have red, blue, and green counters.
- You have 2 more red ones than blue ones.
- You have 3 more green ones than blue ones.
- How many counters of each colour might you have?
- How many counters might there be altogether?



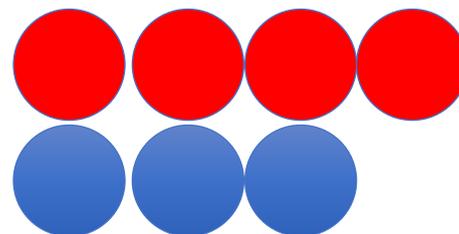
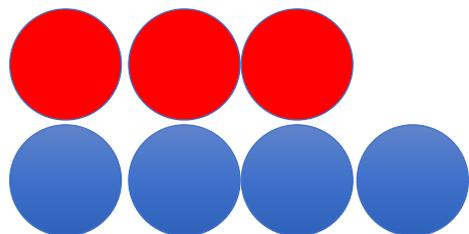
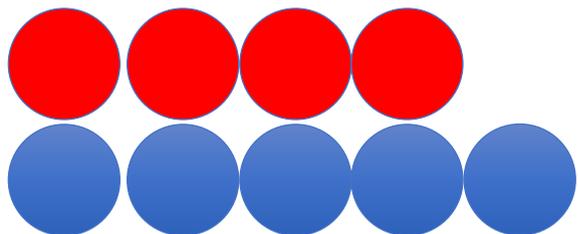
Variation for Grade 1

- Why are the numbers of counters always 8, 11, 14,... and nothing else?

Variation for Grade 3

- You have a bunch of counters.
- Almost half are red.
- How many counters of each colour might you have?

For example



My questions

- Does the number of counters have to be odd or could it be even?
- Could there be, e.g. 3 more reds than non-reds?

A Grade 8 task

- You are multiplying two fractions and the answer is close to one of them.
- What could the fractions be?

A Grade 8 task

- How do I know one of the fractions must be close to 1?
- Do I know if it's bigger or smaller than 1?
- Do I know anything about the other fraction?

A Grade 10 task

- A field was measured in both yards and metres.
- One of the values was 10 more than the other.
- How long was the field?

Questions

- Was the metre number or yard number bigger? Why?
- How do you know the field can't be really short?
- How do you know it can't be super long?

So I wonder?

- Are your teachers being intentional in choosing activities?
- What criteria are they using?

Part 2:

Finding Out Where You Are

Part 2

- An important early activity is to find out what the whole staff, as a group, believes about the teaching of math
- Let's do a little survey you might use.

Part 2

- It might be good to use Poll Everywhere to ensure anonymity, but still see what others think.

Part 2

The big focus in math instruction should be on applications.

Vote: <https://goo.gl/emk5kP>

Results: <https://goo.gl/mjSZ9L>

Part 2

Covering curriculum matters more than making the math interesting to students.

Vote: <https://goo.gl/ZpBcgn>

Results: <https://goo.gl/2xQq4W>

Part 2

Math is mostly about developing computational and algebraic skills.

Vote: <https://goo.gl/RWFt9h>

Results: <https://goo.gl/eLqTAi>

Part 2

Most of my teaching time in math should focus on problem solving.

Vote: <https://goo.gl/BLQ4ox>

Results: <https://goo.gl/y2nZWA>

Part 2

Math is more about procedures than concepts.

Vote: <https://goo.gl/ULkxuk>

Results: <https://goo.gl/3BXPQD>

Part 2

Most math teaching should be direct instruction, with some guided and some exploratory work.

Vote: <https://goo.gl/eBFGQ2>

Results: <https://goo.gl/LjTNs8>

Part 2

The currently weakest students in my class might improve, but really can't be expected to achieve top levels.

Vote: <https://goo.gl/3CYiLu>

Results: <https://goo.gl/7DJLPC>

Part 2

Open-ended problems should be used rarely since they are too hard to give a mark or level to.

Vote: <https://goo.gl/MnJt1i>

Results: <https://goo.gl/vQhJqV>

Part 2

- Now we need to engage in a conversation.
- How much do we agree?
- Do we need to agree? On which points?

Part 2

- The other way to find out where you are is to use common tasks across panels.
- My friend Doug, for example, used these.

Part 2

- Subtraction
- Choose one of these. Show how to get an answer at least three different ways.
- $10 - 3$
- $50 - 29$
- $4.1 - 1.78$
- $8/3 - 2/5$

Part 2

- Or proportional thinking
- Choose one of these. Show how to get an answer at least three different ways.
- **Choices:**
- What is 25% of 396?
- If 8 batteries cost \$3.76, how much should 6 of those same batteries cost?
- You drive 48 mph. How long will it take to go 588 miles?

Part 2

- Or algebraic thinking
- Choose one of these equations. Show three ways to figure out a solution:
 - $\frac{1}{2}x - \frac{2}{3} = \frac{3}{4}x - 2$
 - $3x^2 + 19x - 14 = 0$
 - $-4x - 17 = 2x + 8$
 - $x^2 - 16 = 36$

Part 2

- Looking at student work tells the tale.
- Are students other than procedural?
- Do they use lots of models? Appropriate ones?
- Does the thinking get more sophisticated, without prompting, as students get older?

Part 3:

Look Fors

Part 3

- As a leader, you need to know what it is you want to be happening in the math classroom.
- There are so many “lists”, but what are the biggies?

Part 3

Let's look at Look For List 1.

Part 3

- A debate in Grade 1 might be whether the number 15 is more like 20 or more like 10.
- A debate in Grade 5 might be: Do you think you are more likely to get a 2-digit answer or a 3-digit answer when you divide a 3-digit number by a 1-digit number?

Part 3

- A debate in Grade 9 might be whether lines with higher slopes are always steeper.

Part 3

Or there could be an open question like:

- Are there numbers that are HUGE that don't take a lot of words to say?
- Are there numbers that are SMALL that do take a lot of words to say?

Part 3

Or there could be an open question like:

- Are there irrational numbers that are very little?
- Are there irrational numbers that are very big?

Part 3

Or, instead of:

- Show me 456 with base ten blocks

You hear:

- How could you show 456 with more than 15 blocks?

Part 3

You would be asking questions of children like:

- Do you like to talk about math or would you rather just do it on paper?

You could be facilitating conversation by providing dry-erase paint for tables or multiple white boards so kids can communicate collaboratively.

Part 3

Notice the parallel on the second page in terms of your work with teachers.

Part 3

Your actions:

1. You cannot delegate this if you are a principal or school leader. You must get in there. (I know many of you are VPs, but I think the P needs to be highly involved.)
2. You must make a math change a singular focus and a very visible focus.

Part 3

Your actions:

1. Provide full group and personalized pd based on student data.
2. Use positive change to garner more buy-in.

Part 3

Let's look at Look For List 2.

Part 3

- This is HARD for teachers to do on their own.
- That is why we need collaboration with coaches, math leads, colleagues, and the right resources.

Part 3

- Resources teachers use:
- Why I am nervous about Pinterest, Teachers Pay Teachers, etc.
- Why resources need coherence within grade and across grades

Part 3

So, for example, you want to see:

- Problems that lead to generalizations
- A focus on understanding
- Attention to both extending strong students and supporting strugglers
- Attention to the important ideas in math
- Consolidation focusing on important ideas

Part 3

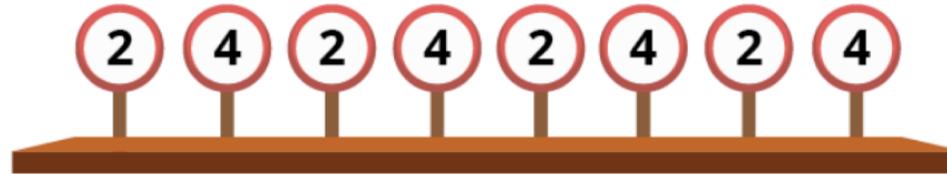
Problems that lead to generalizations

Part 3

For which pattern would you rather predict the 50th term? Why?



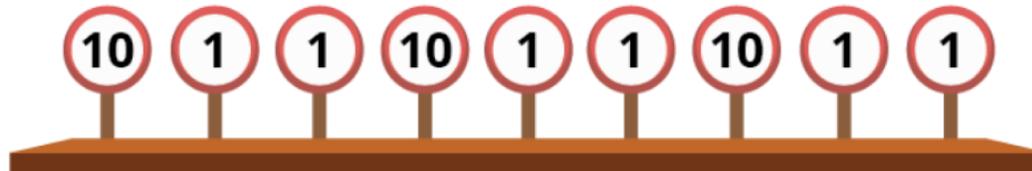
Pattern A



Pattern B



Pattern C



Part 3

A focus on understanding.

Part 3

$\frac{2}{3}$ of one number (call it A) is less than $\frac{1}{3}$ of another number (call it B).

What do you know about A and B?

Part 3

Attention to both extending strong students and supporting strugglers.

Part 3

Suppose the thrust of a lesson in Grade 5 is on recognizing how subtraction of decimals relates to subtraction of whole numbers.

The main task might be:

Part 3

Create two problems.

Problem 1 is solved by subtracting 42 from 105.

Problem 2 is solved by subtracting 0.42 from 1.05.

How are the problems similar and different?

How are the answers similar and different?

Part 3

For struggling students:

You might need to change the numbers to, e.g. 42 and 64 and 4.2 and 6.4.

For strong students:

You might need to ask about 0.42 and 1.5.

Part 3

Attention to the important ideas in math.

Part 3

- Each lesson describes the related essential understanding.

Part 3

ESSENTIAL UNDERSTANDINGS

MEASUREMENT

M-1 Using units when describing a measurement makes it easier to describe and compare it to the measurements of other objects.

M-3 The choice of a measurement unit is affected by many factors, including the precision desired, the user's comfort in making sense of the resulting number of units, and if comparing a measurement with a known measurement, the unit used for the known measurement.

M-4 When two objects are measured using different units, the measurements can still be compared if the relationship between the units is known.

M-5 Estimating is a useful part of the measuring process. Estimating is facilitated by using familiar benchmarks.

M-6 Some measurements of an object are independent of other measurements of that object, but some are related.

Part 3

Consolidation focusing on important ideas.

Part 3

For a lesson focused on mental addition and subtraction.

You present a realistic situation that calls for the use of mental addition and mental subtraction.

Then....

Part 3

After some small group sharing:

- 1.** What two-digit numbers are easy to calculate using mental strategies?
Explain your choices.
- 2. a)** When did you use a strategy where you broke a number into parts?

b) Explain why the strategy works and why it is helpful.
- 3.** Did you ever use both addition and subtraction in a calculation?
If so, describe what you did.
- 4.** Is there always more than one way to add or subtract mentally?
Explain your thinking.

Part 3

Questions 1 and 3 remind students that there is always a variety of strategies that can be called upon, including mental math.

Question 2 encourages students to reflect on Essential Understanding O-7 (the value of decomposing and recomposing numbers to operate with them).

Question 4 asks students to reflect on Essential Understanding O-10 (there are always many strategies for performing a calculation).

Part 3

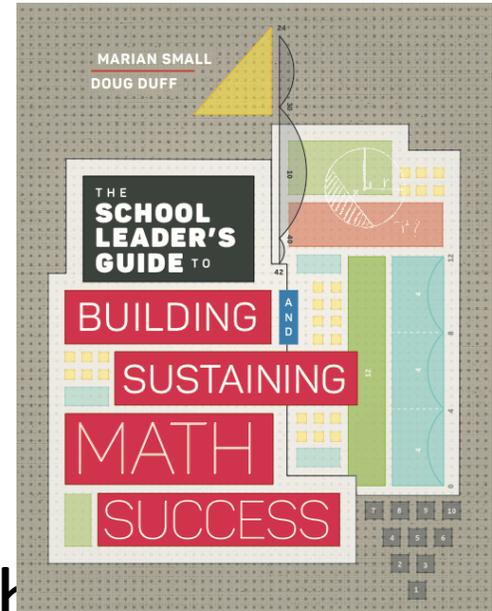
- Let's look, one more time, at Look For List 2.
- Again, there are actions about teachers working with students, but also actions about principals working with teachers.

Part 3

- You also might use “audit tasks” to look for improvement.
- These are tasks quite similar to your common tasks, where you should see growth.

Part 3

- Just so you know-
- Doug Duff and I have written a book for ASCD out in July focused on the role of the principal in changing the math culture and performance in the school.
- Doug is also producing an online program through Rubicon Publishing to support principals.



Part 4:

How Should Lessons Look

Part 4

- The teacher has a learning goal that fits the nuts and bolts of the curriculum but reaches beyond skills toward critical thinking or at least thinking!

Part 4

- For example:
- The goal is not just about multiplying 3-digit numbers by 1-digit numbers, but is about helping kids see how decomposing numbers thoughtfully helps us deal with computations.

Part 4

- The learning goal should derive from bigger ideas or essential understandings.
- The learning goal should help a teacher choose an appropriate task and help them know what to ask in consolidating.

Part 4

- The main problem engages students with interesting problems that pique curiosity, but I do not believe they have to always be real-life.

Part 4

- Or

I might ask kids:

- Is it true that whenever the numerator and denominator of a fraction are closer together, the fraction is bigger?
- And they explore that conjecture.

Part 4

- The consolidation:
 - There needs to be a meaningful consolidation.
 - Its focus is NOT just to share work.
 - Its focus is to evoke the important ideas of the lesson using the children's work and thinking.

Part 4

- Let's look at a Grade 2 example.

Part 4

- Getting ready: Show me 27 with base ten blocks different ways.

Part 4

- Main problem:
- Determine 3 numbers to fit each rule.
- Determine 3 numbers that do not fit each rule.

- Rule 1: The number of ten rods is more than the number of unit cubes.
- Rule 2: There are exactly 3 more one cubes than ten rods.

Part 4

- To consolidate work on Rule 1: The number of ten rods is more than the number of unit cubes.
- Who thinks they have one of the smallest numbers in the room?
- Could it be smaller? Why or why not?
- Who thinks they have one of the greatest numbers in the room?
- Could it be greater? Why or why not?

Part 4

- Suppose a number worked. Would the number with switched digits work? Explain.
- Are most of your answers on the left side or right side of the hundreds chart? Explain.

Part 4

- Having seen what I've done, how would you consolidate Rule 2 (There are 3 more ones blocks than ten rods.)

Part 4

- Let's look at Grade 8 and focus on the division of fractions.
- I might decide that division makes more sense if I think of $a \div b$ as how many b 's fit into a .

Part 4

- So I might get started by:
- There are 10 copies of _____ in _____.
- What could the numbers be if at least one is a fraction?

Part 4

- Main problem:
- Use the fraction tower I gave you.
- Name a fraction that fits into another one this many times:
 - 2 times
 - 3 times
 - 1.5 times
 - 2.5 times
 - $1 \frac{1}{3}$ times

Part 4

- To consolidate:
- What fraction might fit into $\frac{6}{10}$ two times? three times?
- Why does $\frac{1}{3}$ fit into $\frac{1}{2}$ more than 1 but less than 2 times?
How many times?
- How many times does $\frac{2}{10}$ fit into $\frac{3}{10}$? $\frac{2}{8}$ into $\frac{3}{8}$?
- How many times does $\frac{3}{5}$ fit into $\frac{4}{5}$? Why? $\frac{3}{10}$ into $\frac{4}{10}$?

Part 4

- How many times will $5/[]$ fit into $9/[]$? Why?
- Does the value of $[]$ matter?

Part 4

- What you are seeing is being intentional and linking to ideas, not just answers.

Part 4

- What role do admin or coaches play?
- You need to help teachers see the difference between learning goals about doing and learning goals about understanding.
- You need to help teachers see the difference between consolidations that just share and consolidations that bring out ideas.

Part 4

- You need to help teachers look at the difference in student work, particularly on understanding questions, when this becomes the normal approach.

Part 4

- You need to help teachers see that without a focus on meanings, models and particularly decomposition with respect to number, what you want to happen probably won't happen.

Part 5: Your Questions

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