# Supporting your child's math learning 

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## Tonight I will address

$\infty$ How the teaching of math has and has not changed
$\infty$ Things you can do to support your child's math learning
$\propto$ There will certainly be time for questions throughout or at the end.

## There are 5 strands


\& Number
$\infty$ C Geometry
$\propto$ Measurement
$\infty$ Pattern and Algebra
$\propto<$ Data and Probability

## Most of you...


$\propto s$ are most concerned about number, so I will start there.

## Working with numbers

$\infty$ The way we approach the learning of "facts" and the learning of procedures has changed in some ways, but not other ways.
$a_{8}$ We will discuss both the how and the why.

## Facts first


© Facts are things like $4+8=12$ or $7 \times 4=28$ or $12-3=9$ or $40 \div 5=8$.
\& They involve small numbers.
$\propto<$ Facts remain important because they are fundamental both to estimation and any other calculations.

## We used to believe...


$\infty$ The best way to learn facts is to sit down and memorize them by saying them over and over.
$\propto<$ And that being super fast with them is really important.

## Now we realize...

$\leftrightarrow$ \& That you are ahead of the game if you have tools to recall something you have memorized but may forget.
$\propto<$ We call these strategies.

## An added benefit..


$\propto$ Q The strategies we use to help kids recall facts also are useful in other computations.

## There is now research that shows...


$\bigcirc$ P That even though some kids memorize well..
$\infty$ for kids who are anxious about math or get nervous having to be quick, old strategies doom them to failure.
$\infty$ Brain research shows that when you are anxious, it is short term memory that is impacted and that is where facts are stored. (Sian Bellock)
$\infty$ We need to approach fact learning in different ways for different kids.

## So we teach principles and strategies <br> 

$\propto \&$ For example, since 4 combined with 5 is the same as 5 combined with 4 , we only have to learn half the addition facts.

## So we teach principles and strategies <br> 

$\infty$ For example, since 8 combined with 3 is the same $8+2$ +1 , it' s really $10+1$

| O | O | O | O | O |
| :--- | :--- | :--- | :--- | :--- |
| O | O | O | X | X |


| $\mathbf{X}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |

## So we teach principles and strategies


$\propto$ For some reason, we learn doubles quickly, so kids can relate $3+4$ to $(3+3)+1$ or $(4+4)-1$.
$\propto$ Or $7+8$ to $(7+7)+1$ or $(8+8)-1$.

## So we teach principles and strategies

$\leftrightarrow 8$ For example, since 4 groups of 5 can be viewed as 5 groups of 4, we only need to memorize half the multiplication facts.
0
0
0
0
0
0
0
0
0
0
0
0
0
0
0
$\begin{array}{lllll}0 & 0 & 0 & 0 & 0\end{array}$

## So we teach principles and strategies

$\propto$ For example, since 4 groups of 7 can be viewed as 4 groups of 5 with 4 groups of 2, we know the $7 x$ table if we can learn the 5 x and 2 x tables.

| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{x}$ | $\mathbf{x}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{x}$ | $\mathbf{x}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{x}$ | $\mathbf{x}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{x}$ | $\mathbf{x}$ |

Many of these principles

## can be..


$\infty$ Seen on addition and multiplication tables
CR visualized using manipulatives

| + | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| $\mathbf{2}$ | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| $\mathbf{3}$ | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| $\mathbf{4}$ | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| $\mathbf{5}$ | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| $\mathbf{6}$ | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| $\mathbf{7}$ | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| $\mathbf{8}$ | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| $\mathbf{9}$ | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |


| $\times$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 0 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| 3 | 0 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 |
| 4 | 0 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 |
| 5 | 0 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 |
| 6 | 0 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 |
| 7 | 0 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 |
| 8 | 0 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 |
| 9 | 0 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 |


| $\times$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 0 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| 3 | 0 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 |
| 4 | 0 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 |
| 5 | 0 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 |
| 6 | 0 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 |
| 7 | 0 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 |
| 8 | 0 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 |
| 9 | 0 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 |

## Math tools

\& 10-frames


It's easy to see why $9+9=10+8$ (18).

Just move one counter up.

## Accessing virtual manipulatives <br> 

\& There are tools for materials your children use in class freely available on line.
$\propto \times$ Many are also available as apps.

## Pattern Blocks

$\infty$ http://nlvm.usu.edu/en/nav/
frames_asid_169_g_1_t_2.html?open=activities

## Hundreds chart


$\infty$ http://nlvm.usu.edu/en/nav/category_g_2_t_1.html

## Base ten blocks

$\infty$ \&ttp://nlvm.usu.edu/en/nav/category_g_2_t_1.html

## Geometric shapes


\& http://illuminations.nctm.org/Activity.aspx?id=3521

What about computing with 2digit or larger numbers

$\propto$ There is increasingly more focus on estimation and more focus on calculation using strategies, often mentally

## Adding on a 100 chart


$44+32$

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 4 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 44 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 4 | 75 | 79 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## Subtracting on a 100 chart



65-19

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 4 | 4 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## Alternative strategies that might seem new


cos How would you calculate 342-121?
$\infty$ Would you do $200-2$ the same way?
\& Children are learning different strategies since different ones are more efficient or more meaningful in different situations AND
$\propto<$ Different ones make more sense to different kids.

## For example

$\propto$ It is reasonable and correct to add like this:
38
$+\underline{47}$
70
$+\underline{15}$
85

## For example

$\propto$ It is reasonable and correct to add like this:
38
$+\underline{47}$

$$
=38+50-3=88-3=85
$$

## Or subtract like this...



$$
\begin{aligned}
\text { c } 100 & =99+1 \\
-79 & \underline{-79} \\
& 20+1=21
\end{aligned}
$$

## Strategies also are useful in multiplying <br> 

cs For example:


## Also division

$\mathrm{C}_{8}$ How many packages of 8 cookies if there are 348 cookies to package?

| 8 | 348 <br> -80 |
| ---: | ---: |
| 268 | 10 |
| $-\underline{160}$ | 20 |
| 108 |  |
| $-\underline{80}$ | 10 |
| 28 |  |
| $-\underline{24}$ | $\underline{3}$ |
| 4 | 43 |

## Attention to estimation


$\propto_{8}$ In the world toward which we are moving, technology will be regularly used to calculate, but we still need to estimate to see if those answers make sense.

## Attention to estimation

$\infty$ Is $42+58+91$ closer to 100,150 or 200 ? Why?
\& About how much is 4213-3314?
$\propto 8$ Why is $29 \times 42$ close to 1200 ?

## Other strands


© Algebra work earlier, particularly things like:

$$
4+[]=5+8
$$

## Teaching through problem solving <br> 

$\infty$ R This is a better description of what we do than "discovery".
$\propto$ It means that as we solve a problem, we clarify a lot of ideas.

## I might ask...



Cs I bought something and gave the clerk $\$ 10$.
$\infty$ She gave me back one bill and 4 coins.
co How much might the item have cost?

## Lots of thinking

as Realizing that the bill has to be $\$ 5$.
© Realizing that the coins, these days, have to be nickels, dimes, quarters, loonies or toonies.

Qs Getting lots and lots of practice trying lots and lots of combinations.

C R Realizing that the price + the change $=\$ 10$

## What can you do?


$)_{8}$ Our big question as parents is what we can do to help our child.

## Number Play



Lots of children respond well to "magic".
For example:

- Choose a number.
( Double it.
- Add 4.
- Double that.
- Add 8.
- Divide by 4.

Tell me your answer and I will guess your
number.

## How did I make that up?


$\propto$ Choose a number.
CP Double it. $\square$
cr Add 4.
© Double that.
$\square$
$\square$
$\square$
© A Add 8.

## $\square \square+4$

$$
+8
$$

$$
+16
$$

CR Divide by 4 .
$+4$

## How many....?


$\leftrightarrow 8$ Spoons in the drawer?
\& Steps to get downstairs?
$\infty$ Trees on the street?
$\propto$ Qections in an orange?
CR Windows in the house?

## Interesting Questions


@ Ask little questions in passing.
\& e.g. The answer is 10 . What is the question?
$\infty$ If McDonalds' s sells McNuggets in packs of 6,9 and 20 , can you buy exactly $25 \mathrm{McNuggets?}$

## Support involves...

$\propto<$ Not showing, but probing.
$\propto$ Asking why this or why that...
\& Building connections

## Games


$\propto \&$ You could play games where you make up the rules or use existing games to practise skills.

## Games to Play

$\infty 2$ players
$\propto$ Each rolls two dice. The score is the sum.
$\propto \times$ The first player to get to 100 wins.

## Games to Play


\& 2 players
$\infty$ Each rolls two dice. The score is 2 x one value + the other.
$\propto$ The first player to get to 100 wins.

## Board games


$\bigcirc 24$

# Box cars and one eyed jacks 


© $\rightarrow$ http://www.boxcarsandoneeyedjacks.com/

You could solve interesting problems


# How much is your name worth? 



| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}$ | $\mathbf{E}$ | $\mathbf{F}$ | $\mathbf{G}$ | $\mathbf{H}$ | $\mathbf{I}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| $\mathbf{J}$ | $\mathbf{K}$ | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{N}$ | $\mathbf{O}$ | $\mathbf{P}$ | $\mathbf{Q}$ | $\mathbf{R}$ |
| 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| $\mathbf{S}$ | $\mathbf{T}$ | $\mathbf{U}$ | $\mathbf{V}$ | $\mathbf{W}$ | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{Z}$ |  |
| 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 |  |

What words are worth 40 50?


| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}$ | $\mathbf{E}$ | $\mathbf{F}$ | $\mathbf{G}$ | $\mathbf{H}$ | $\mathbf{I}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| $\mathbf{J}$ | $\mathbf{K}$ | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{N}$ | $\mathbf{O}$ | $\mathbf{P}$ | $\mathbf{Q}$ | $\mathbf{R}$ |
| 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| $\mathbf{S}$ | $\mathbf{T}$ | $\mathbf{U}$ | $\mathbf{V}$ | $\mathbf{W}$ | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{Z}$ |  |
| 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 |  |

## Figure this



C8 http://www.figurethis.org

## What is success?


$\propto 8$ Not just a mark
© Enjoying the math
$\propto<$ Making sense of the world using math
\& Building connections

## You need to...


$\propto 8$ Encourage kids to "teach you" what they learned or explain their thinking to you.

## You need to...



Q Show that you enjoy math too.
Q Show confidence- believe that they can if you give them the tim.
$C$ Emphasize good thinking, not speed.
$\infty$ Emphasize the good thinking, not the mistakes.

# You might have questions 

## You can download at



CR Www.onetwoinfinity.ca
cos Parents

